## Lecture 4

## Examples of TMs and Computers vs Turing machines

## Turing Machine for Parity

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## Example: Construct a TM for PARITY $=\{x \mid x$ is a binary string with odd number of 1 s$\}$

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- Two tapes.


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| $\triangleright$ | 0 | 0 | 1 | 0 | 1 | 1 | $\sqcup$ | $\sqcup$ | $\ldots$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

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Solution: • $\delta:\left(q_{\text {start }} \triangleright, \triangleright, \triangleright\right)=\left(q_{\text {copy }}, \triangleright, \triangleright, R, R, R\right)$

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\left(q_{c o p y}, 0, \sqcup, \sqcup\right)=\left(q_{c o p y}, 0, \sqcup, R, R, S\right)
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\left(q_{c o p y}, 0, \sqcup, \sqcup\right)=\left(q_{c o p y}, 0, \sqcup, R, R, S\right) \quad\left(q_{\text {copy }}, 1, \sqcup, \sqcup\right)=\left(q_{\text {copy }}, 1, \sqcup, R, R, S\right)
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\begin{aligned}
& \left(q_{c o p y}, 0, \sqcup, \sqcup\right)=\left(q_{c o p y}, 0, \sqcup, R, R, S\right) \quad\left(q_{c o p y}, 1, \sqcup, \sqcup\right)=\left(q_{c o p y}, 1, \sqcup, R, R, S\right) \\
& \left(q_{c o p y}, \sqcup, \sqcup, \sqcup\right)=\left(q_{l e f t}, \sqcup, \sqcup, L, L, S\right)
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& \left(q_{c o p y}, \sqcup, \sqcup, \sqcup\right)=\left(q_{l e f t}, \sqcup, \sqcup, L, L, S\right) \\
& \left(q_{l e f t}, 0 / 1,0 / 1, \sqcup\right)=\left(q_{l e f t}, 0 / 1, \sqcup, L, S, S\right)
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& \left(q_{c o p y}, \sqcup, \sqcup, \sqcup\right)=\left(q_{l e f f}, \sqcup, \sqcup, L, L, S\right) \\
& \left(q_{l e f t}, 0 / 1,0 / 1, \sqcup\right)=\left(q_{l e f t}, 0 / 1, \sqcup, L, S, S\right) \quad\left(q_{l e f t}, \triangleright, 0 / 1, \sqcup\right)=\left(q_{c o m p}, 0 / 1, \sqcup, R, S, S\right)
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& \left(q_{c o p y}, \sqcup, \sqcup, \sqcup\right)=\left(q_{l e f f}, \sqcup, \sqcup, L, L, S\right) \\
& \left(q_{l e f t}, 0 / 1,0 / 1, \sqcup\right)=\left(q_{l e f t}, 0 / 1, \sqcup, L, S, S\right) \quad\left(q_{l e f t}, \sqcup, 0 / 1, \sqcup\right)=\left(q_{c o m p}, 0 / 1, \sqcup, R, S, S\right) \\
& \left(q_{c o m p}, 0,0, \sqcup\right)=\left(q_{c o m p}, 0, \sqcup, R, L, S\right) \quad\left(q_{c o m p}, 1,1, \sqcup\right)=\left(q_{c o m p}, 1, \sqcup, R, L, S\right)
\end{aligned}
$$

## Turing Machine for Palindrome

Example: Construct a TM for PALIN $=\{x \mid x$ is a palindromic binary string $\}$
Solution: • $\delta:\left(q_{\text {start }} \triangleright, \triangleright, \triangleright\right)=\left(q_{\text {copy }}, \triangleright, \triangleright, R, R, R\right)$

$$
\begin{aligned}
& \left(q_{c o p y}, 0, \sqcup, \sqcup\right)=\left(q_{c o p y}, 0, \sqcup, R, R, S\right) \quad\left(q_{c o p y}, 1, \sqcup, \sqcup\right)=\left(q_{c o p y}, 1, \sqcup, R, R, S\right) \\
& \left(q_{c o p y}, \sqcup, \sqcup, \sqcup\right)=\left(q_{l e f t}, \sqcup, \sqcup, L, L, S\right) \\
& \left(q_{l e f t}, 0 / 1,0 / 1, \sqcup\right)=\left(q_{l e f t}, 0 / 1, \sqcup, L, S, S\right) \quad\left(q_{l e f t}, \triangleright, 0 / 1, \sqcup\right)=\left(q_{c o m p}, 0 / 1, \sqcup, R, S, S\right) \\
& \left(q_{c o m p}, 0,0, \sqcup\right)=\left(q_{c o m p}, 0, \sqcup, R, L, S\right) \quad\left(q_{c o m p}, 1,1, \sqcup\right)=\left(q_{c o m p}, 1, \sqcup, R, L, S\right) \\
& \left(q_{c o m p}, 1,0, \sqcup\right)=\left(q_{\text {halt }}, 0,0, S, S, S\right)
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& \left(q_{c o p y}, 0, \sqcup, \sqcup\right)=\left(q_{c o p y}, 0, \sqcup, R, R, S\right) \quad\left(q_{c o p y}, 1, \sqcup, \sqcup\right)=\left(q_{c o p y}, 1, \sqcup, R, R, S\right) \\
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& \left(q_{c o m p}, 0,0, \sqcup\right)=\left(q_{c o m p}, 0, \sqcup, R, L, S\right) \quad\left(q_{c o m p}, 1,1, \sqcup\right)=\left(q_{c o m p}, 1, \sqcup, R, L, S\right) \\
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& \left(q_{\text {comp }}, 0,0, \sqcup\right)=\left(q_{c o m p}, 0, \sqcup, R, L, S\right) \quad\left(q_{c o m p}, 1,1, \sqcup\right)=\left(q_{c o m p}, 1, \sqcup, R, L, S\right) \\
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Q: Can we solve PALIN using two tapes?

## Computer vs Turing Machine

## Computer vs Turing Machine

Simulating a Computer by Turing machine

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- Add or multiply the content of two registers into some register.


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| $r e g_{1}$ | $r e g_{2}$ | $\cdots$ |
| :--- | :--- | :--- |

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- Executing instructions using $\delta$.


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Simulating a Turing machine by Computer

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A C program with infinite memory can be written that simulates a Turing machine where:

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- High-level languages are used to demonstrate an effective procedure that decides a given language because they are user-friendly.
- Turing machines are used to prove non-existence of an (efficient) effective procedure that decides a given language because of their simple mathematical structure.

